# LOYOLA COLLEGE (AUTONOMOUS), CHENNAI - 600 034 **M.Sc.** DEGREE EXAMINATION - **PHYSICS** FIRST SEMESTER - APRIL 2013 PH 1815/1810 - STATISTICAL MECHANICS Date : 06/05/2013 Dept. No. Max.: 100 Marks Time : 9:00 - 12:00

## PART A

## Answer ALL questions

- 1. Write down the form of second law of thermodynamics for a system for which the number of particles in not a constant.
- 2. State any two postulates of Statistical Mechanics.
- Write down the canonical partition function of a two level system of energies 0 and  $\varepsilon$ . 3.
- Distinguish between canonical and grand canonical ensemble. 4.
- Why does <sup>4</sup>He show super-fluidity at very low temperatures? 5.
- 6. What would be the pressure exerted by a Boson gas on the walls of the container at absolute zero? Justify your answer.
- 7. Define Fermi energy.
- 8. Sketch the Fermi-Dirac distribution law for an ideal gas at absolute zero and at a temperature slightly above absolute zero.
- 9. Define mean square deviation.
- 10. State Nyquist theorem.

### PART B

### Answer any **FOUR** questions

- 11. Obtain the condition for chemical equilibrium between two systems.
- 12. State and prove equipartition theorem.
- 13. Apply the BE statistics to photons and obtain Planck's formula for the energy density of black body radiation.
- 14. Derive an expression for the electronic contribution to specific heat capacity of a metal. Why is this contribution insignificant at high temperature?
- 15. Obtain expression for the concentration fluctuation in a grand canonical ensemble. Show that for an ideal gas it increases as the volume decreases.



 $4 \ge 7.5 = 30$ 

 $10 \ge 2 = 20$ 

### PART C

Answer any FOUR questions

#### $4 \ge 12.5 = 50$

- 16. State and prove Liouville's theorem. Use it to arrive at the principle of conservation of density in phase space.
- 17. a) Obtain Grand canonical distribution function.
  - b) Consider an ideal gas in grand canonical ensemble. Show that its fugacity is directly proportional to concentration.
- 18. Explain the super-fluidity of liquid helium using the spectrum of phonons and rotons.
- 19. What is second sound? Obtain an expression for it based on the two-fluid model.
- Obtain the expressions for the mean square velocity and mean square displacement of a Brownian particle employing method of random walk. Graphically represent the variation of these quantities with time